Math III Geometry Review

Circles

Equation of a circle $(x - h)^2 + (y - k)^2 = r^2$ where (h, k) is the center and r is the radius

A tangent line and the radius of a circle form a 90° angle.

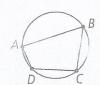
$$\underbrace{\overrightarrow{AB}}_{AB} \text{ is tangent to } \bigcirc O \text{ at } P$$

$$\overrightarrow{AB} \perp \overrightarrow{OP}$$





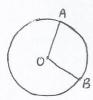
The opposite angles of a quadrilateral inscribed in a circle are supplementary



An angle inscribed in a semicircle is a right angle

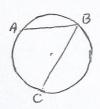


Central Angle



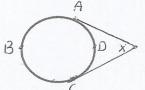
The measure of a central angle Is equal to the arc it opens to

Inscribed Angle

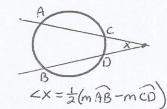


The measure of the inscribed angle is $\frac{1}{2}$ of the arc it opens to

Circumscribed Angles



$$\angle X = \frac{1}{2} (m \widehat{ABC} - m \widehat{ADC})$$



 $\frac{c}{c} = \frac{1}{2} (mAc - mAB)$

Area of a sector

$$\frac{degree}{360}\pi r^2$$

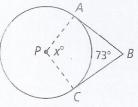
$$\frac{degree}{360} 2\pi r$$

1. \overline{AB} and \overline{BC} are tangent to $\bigcirc P$. What is the value of x.

B. 107

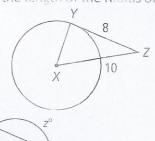
C. 117

D. 146



2. \overline{YZ} is tangent to $\bigcirc X$, and X is the center of the circle. What is the length of the radius of the circle?

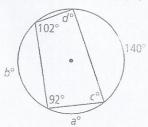
- A. 4
- B. 6
- C. 12
- D. 12.8



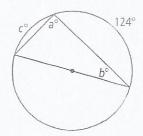
- 3. What is value of z?
 - A. 77
- B. 95
- C. 126
- D. 154

90°

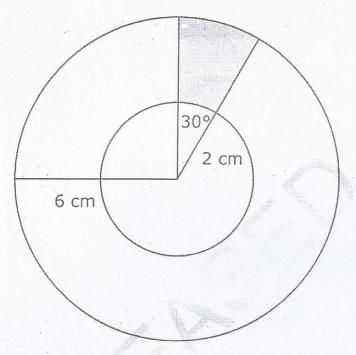




5. What is the value of a, b, and c?



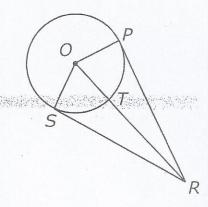
6. In the figure below, the larger circle has a radius of 6 cm, and the smaller circle has a radius of 2 cm.



What is the approximate area of the shaded region?

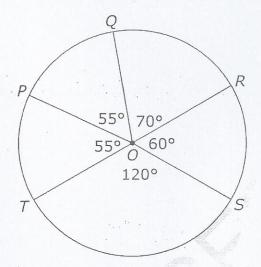
- A 2.1 cm²
- B 3.4 cm²
- C 4.2 cm²
- D 8.4 cm²

7. In the figure below, \overline{PR} and \overline{SR} are tangent to circle O.



If OT = 11 cm and PR = 60 cm, what is the length of \overline{OR} ?

- A 61 cm
- B 59 cm
- C 50 cm
- D 48 cm
- 8. \overline{TR} is a diameter of circle O and has a length of 16 ft.



What is the **approximate** area of the sector bounded by $\angle POR$ and \widehat{PQR} ?

- A 70 ft^2
- B 67 ft^2
- C 42 ft²
- D 39 ft^2

9. Derive the standard equation of the circle $x^2 + y^2 + 4x - 6y = -4$

10. Which is the equation of a circle with center (-2, 3) and a radius r = 5?

A.
$$(x+2)^2 + (y-3)^2 = 10$$

C.
$$(x-2)^2 + (y+3)^2 = 10$$

B.
$$(x+2)^2 + (y-3)^2 = 25$$

A.
$$(x+2)^2 + (y-3)^2 = 10$$

B. $(x+2)^2 + (y-3)^2 = 25$
C. $(x-2)^2 + (y+3)^2 = 10$
D. $(x-2)^2 + (y+3)^2 = 25$

11. Which of the following is the graph of $(x-2)^2 + (y+1)^2 = 9$



